



Exam Score:

/20

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*Mohd
Answer*

Try the following Problems

Problem I

/4

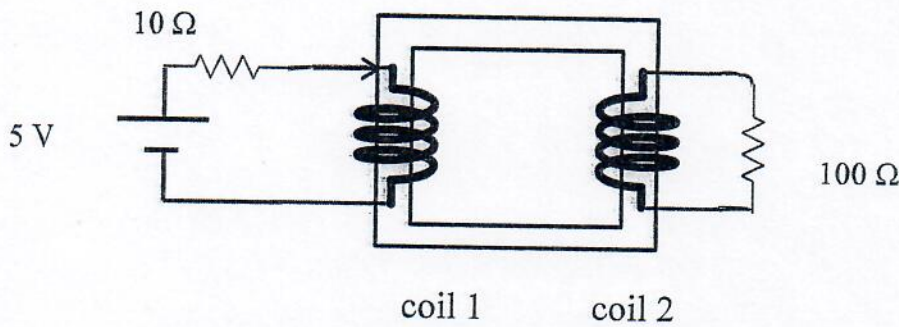
The magnetic circuit shown has the following:

$N_1 = 50$ turns, $N_2 = 20$ turns, iron core length, $l_c = 40$ cm

iron core cross section area = $4\text{cm} \times 4\text{cm}$ where $\mu_r = 50000$

Coil 1 connected to a 5V battery and resistor 10Ω and coil 2 is connected to a 100Ω resistance. Find

- (a) L_{12}
- (b) Power delivered by the battery at steady state



$$L_{12} = \frac{\mu_0 \mu_r N_1 N_2 A_c}{l_c} = \frac{4\pi \times 10^{-7} \times 50,000 \times 50 \times 20 \times 16 \times 10^{-4}}{40 \times 10^{-2}}$$

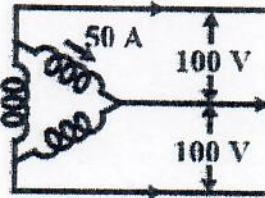
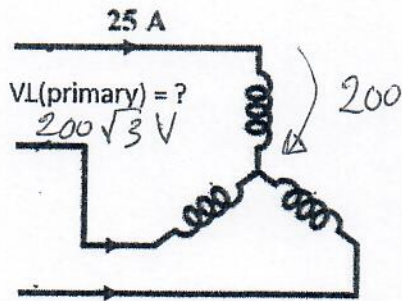
(2)

$$= 251 \text{ mH}$$

(a) steady state $P = \frac{V^2}{R} = \frac{25}{10} = 2.5 \text{ W}$ (2)

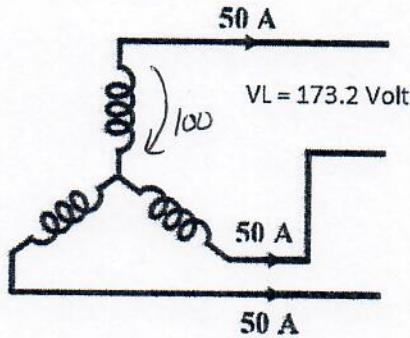
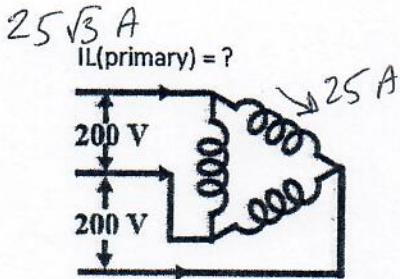
Problem II

In the following 3 phase ideal transformers, supply the missing line and phase currents and voltages



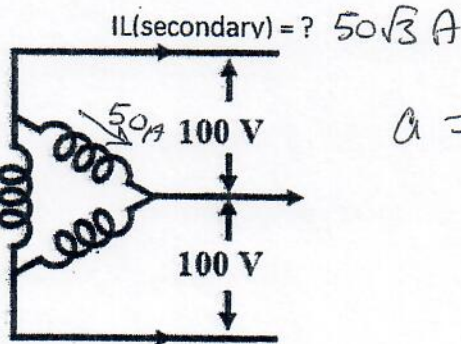
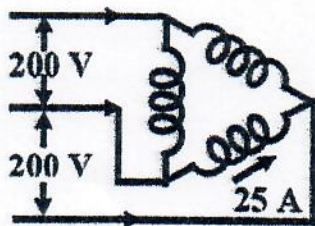
$a = 2$

(1.5)



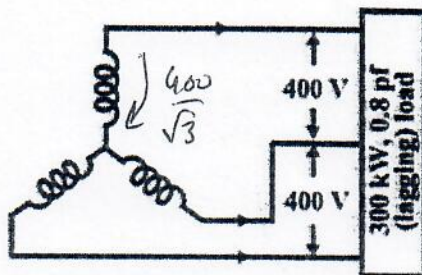
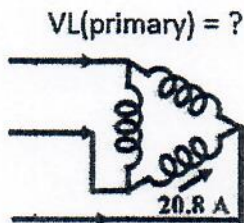
$a = 2$

(1.5)



$a = 2$

(1.5)



$300 \times 10^3 = \sqrt{3} \times 400 \times I_L \times 0.8$

$I_L = 541.3 \text{ A}$

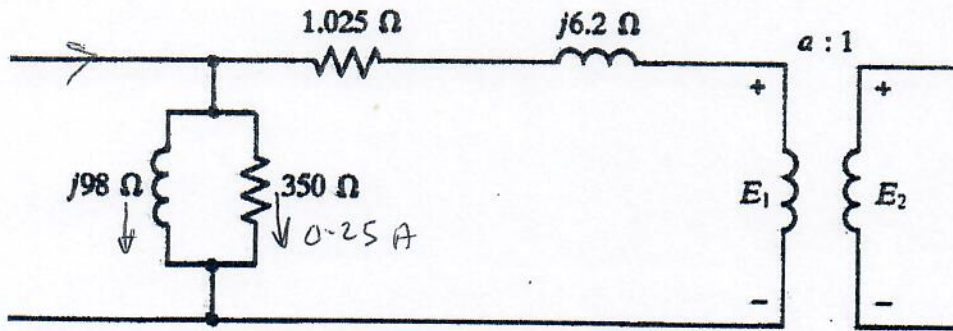
$a = \frac{541.3}{20.8} = 26$

$V_{L \text{ pri}} = 26 \times \frac{400}{\sqrt{3}} = 6004 \text{ V}$

(1.5)

Problem III

For the transformer equivalent circuit shown, the secondary is open circuit, $a = 5$, and the current in the 350Ω is 0.25 A . Find V_1 , V_2 , I_1 , I_2 , total power losses, and the transformer efficiency η .



$$V_1 = 0.25 \times 350 = 87.5 \angle 0 \text{ V} \quad \left(\frac{1}{2}\right)$$

$$i_x = \frac{87.5}{98} = 0.89 \angle -90 \text{ A}$$

$$I_1 = 0.25 \angle 0 + 0.89 \angle -90 = 0.92 \angle -74.3^\circ \text{ A} \quad (1)$$

$$I_2 = 0 \quad \left(\frac{1}{2}\right)$$

$$E_1 = V_1$$

$$E_2 = V_2 = \frac{1}{5} \times 87.5 \angle 0 = 17.5 \angle 0 \text{ V} \quad \left(\frac{1}{2}\right)$$

$$\text{total power loss} = (0.25)^2 \times 350 = 21.9 \text{ W} \quad (1)$$

$$\eta = 0 \quad \left(\frac{1}{2}\right)$$

Problem IV

A single-phase 1000/200 V transformer undergoes two tests:

- (i) The primary no-load current is 3 A at 1000 V and a power factor of 0.2 lagging.
- (ii) The primary current is 24 A at 1000 V and a power factor of 0.7 lagging when the secondary current is 100 A at 200 V and a power factor of 0.8 lagging.

Assuming iron loss is the same in the two tests, find:

- (a) Iron loss
- (b) Copper loss in each case
- (c) The transformer efficiency in each case

$a = 5$

(i) iron loss = $3 \times 1000 \times 0.2 = \boxed{600 \text{ W}}$ ~~\times~~ $\boxed{\text{Copper loss} = 0}$

(ii) input power = $24 \times 1000 \times 0.7 = \boxed{16800 \text{ W}}$

output power = $100 \times 200 \times 0.8 = \boxed{16000 \text{ W}}$

$\sum \text{losses} = \boxed{800 \text{ W}}$ (1)

\therefore Copper loss = $800 - 600 = \boxed{200 \text{ W}}$ (1)

$\eta_1 = 0$ (1)

$\eta_2 = \frac{16000}{16800} \times 100 = \boxed{95.2 \%}$ (1)